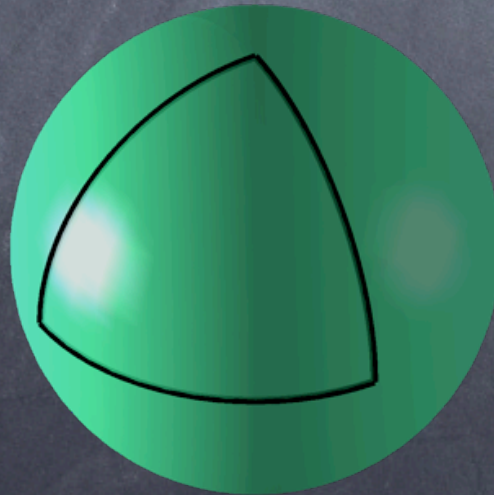
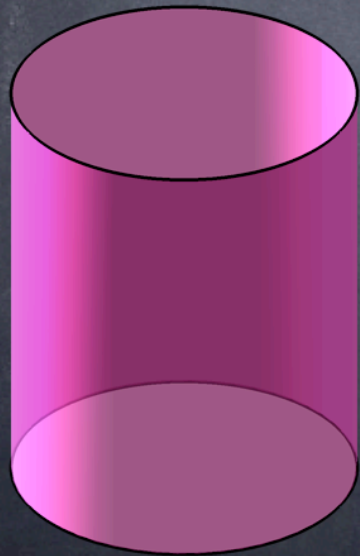
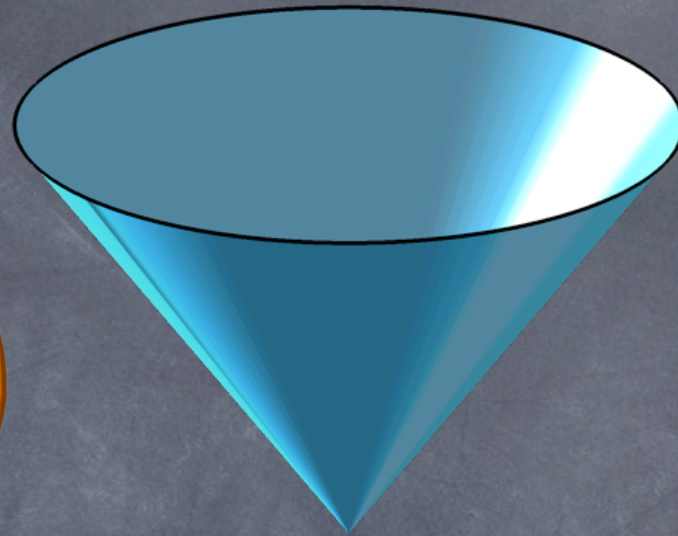


# Intrinsic and extrinsic curvature



Intrinsic curvature  
measured by the  
Riemann tensor

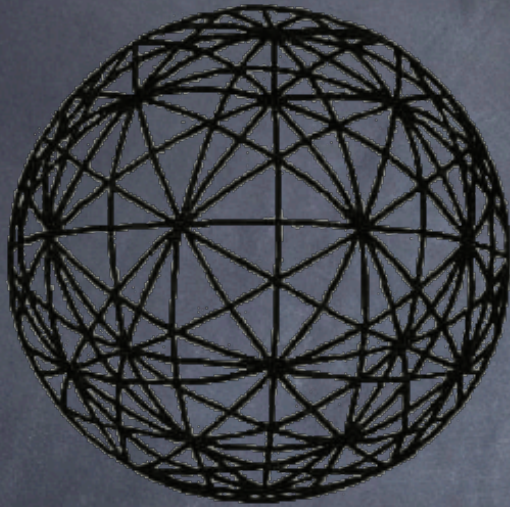
$$R_{abc}{}^d$$

Dimension of  $R_{abc}{}^d$

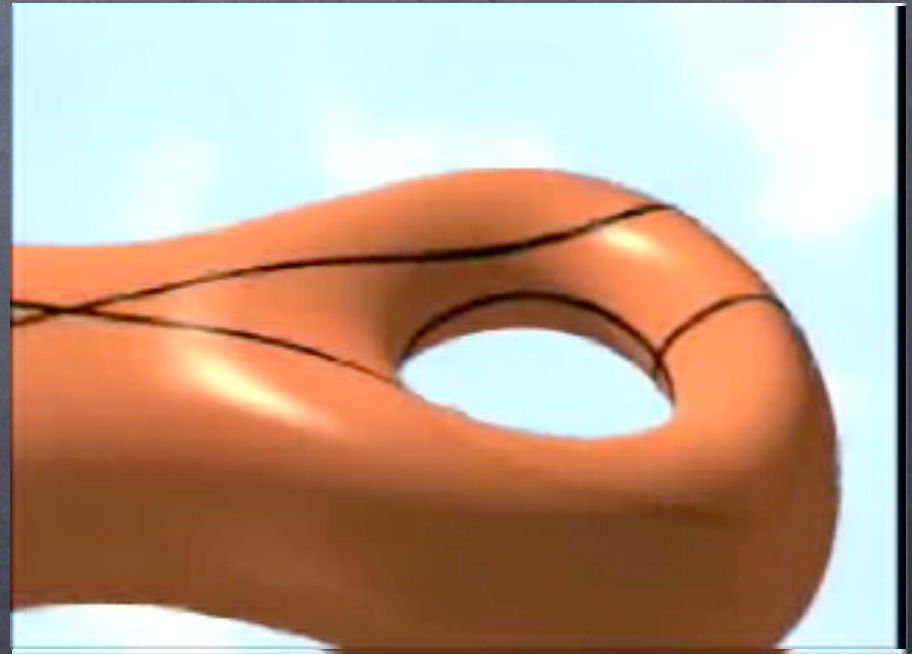
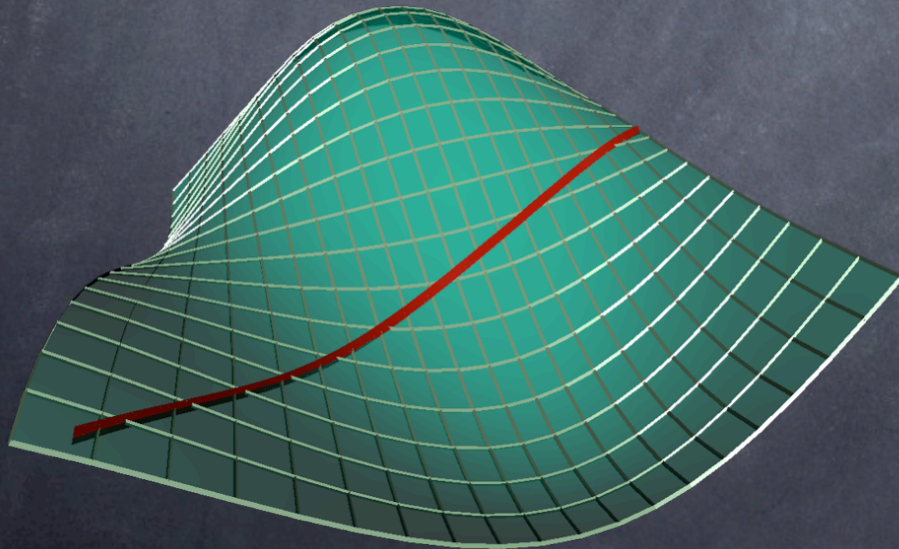
1-D	0
2-D	1
3-D	6
4-D	20

# Geodesics

Straight lines through curved space

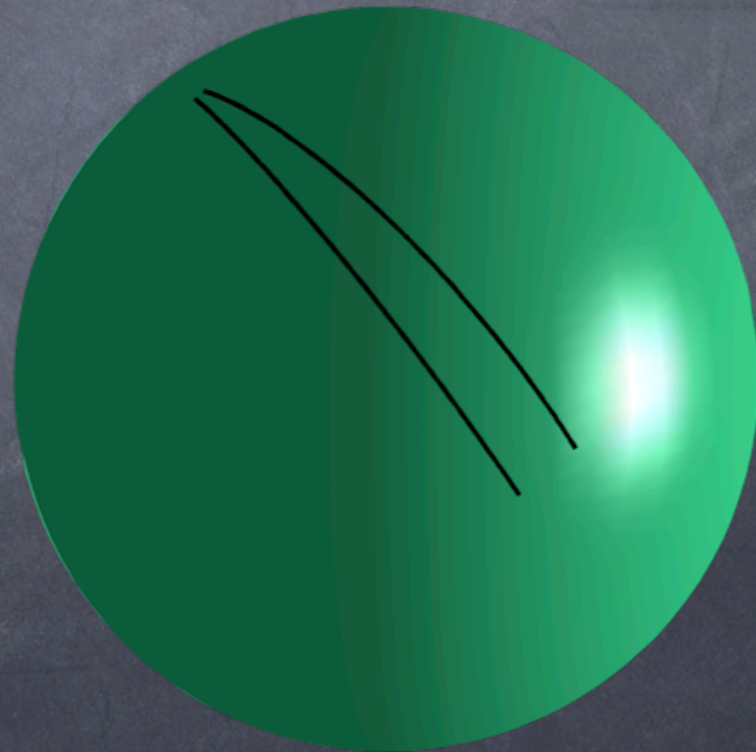
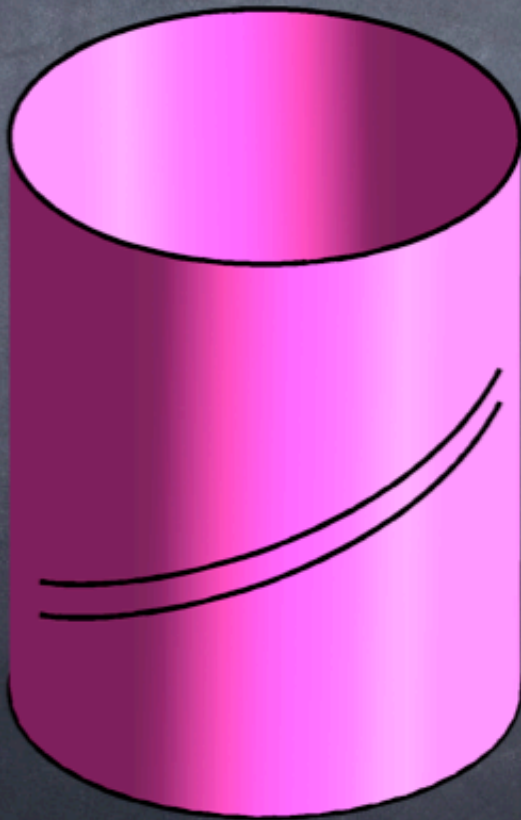


Objects in free fall move on the straightest possible paths through curved spacetime

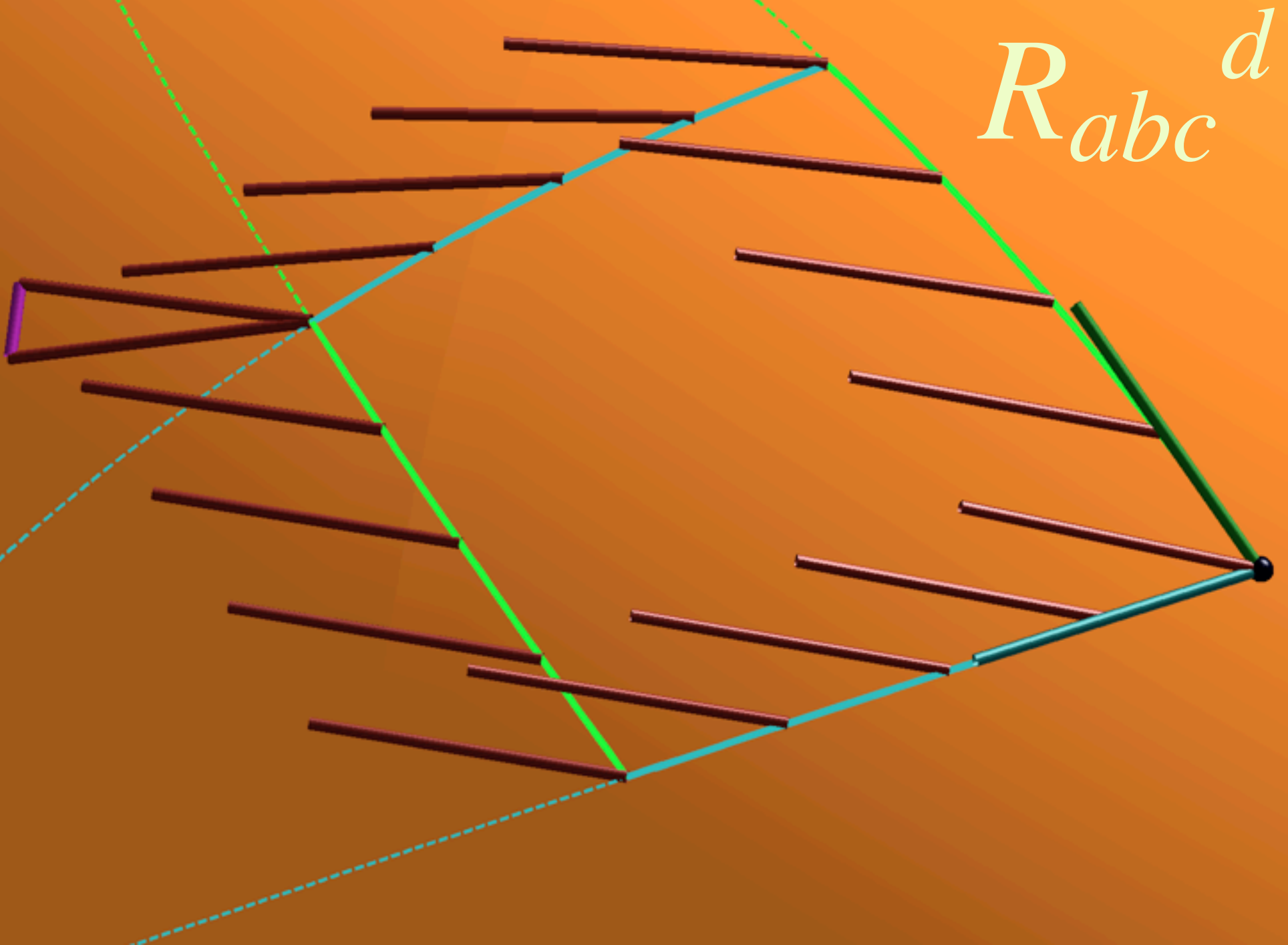


# Geodesic deviation

Spreading or convergence of parallel geodesics can be used to measure intrinsic curvature.



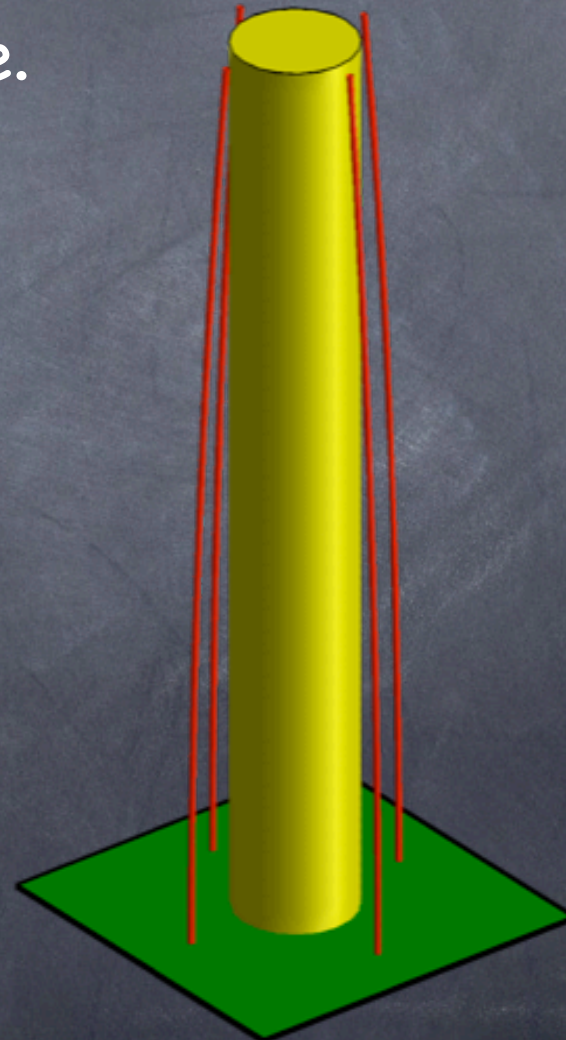
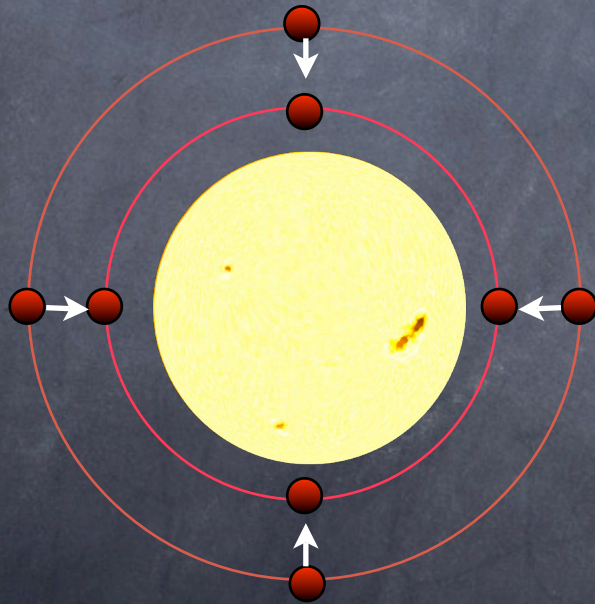
# Riemann curvature tensor



# Ricci curvature

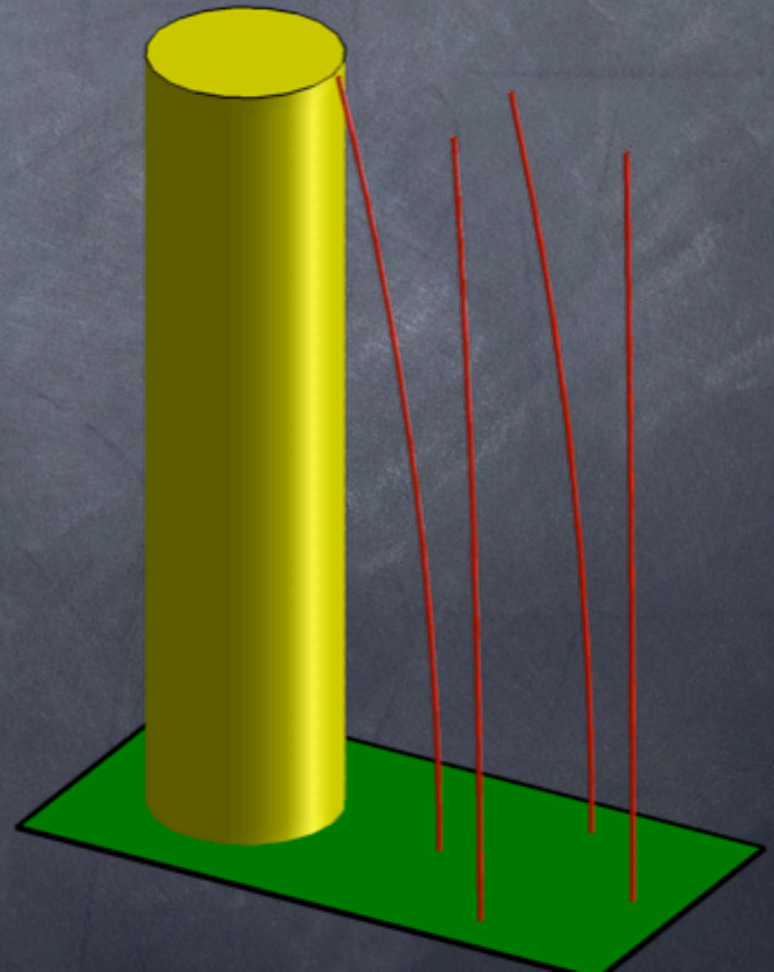
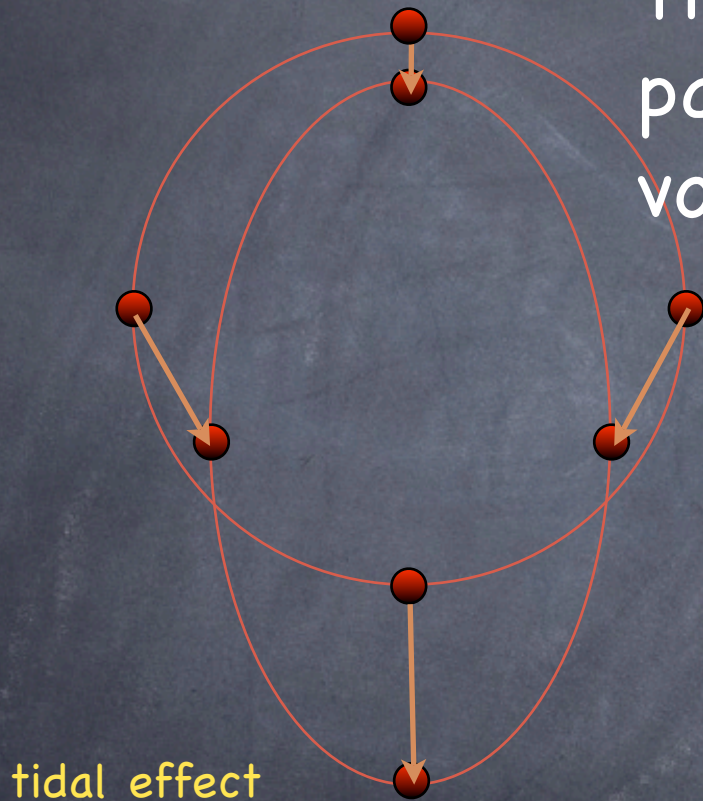
Ricci curvature is the trace of the Riemann tensor, the part responsible for volume change.

$$R_{ab} = R_{adb}{}^d$$



# Weyl curvature


The Weyl tensor is the trace-free part of Riemann, responsible for volume-preserving shape distortion.



# Einstein's field equations

$$R_{ab} = kT_{ab}$$

Mass-energy tensor,  
comes from a matter model,  
vanishes for vacuum



almost...

# Einstein's field equations

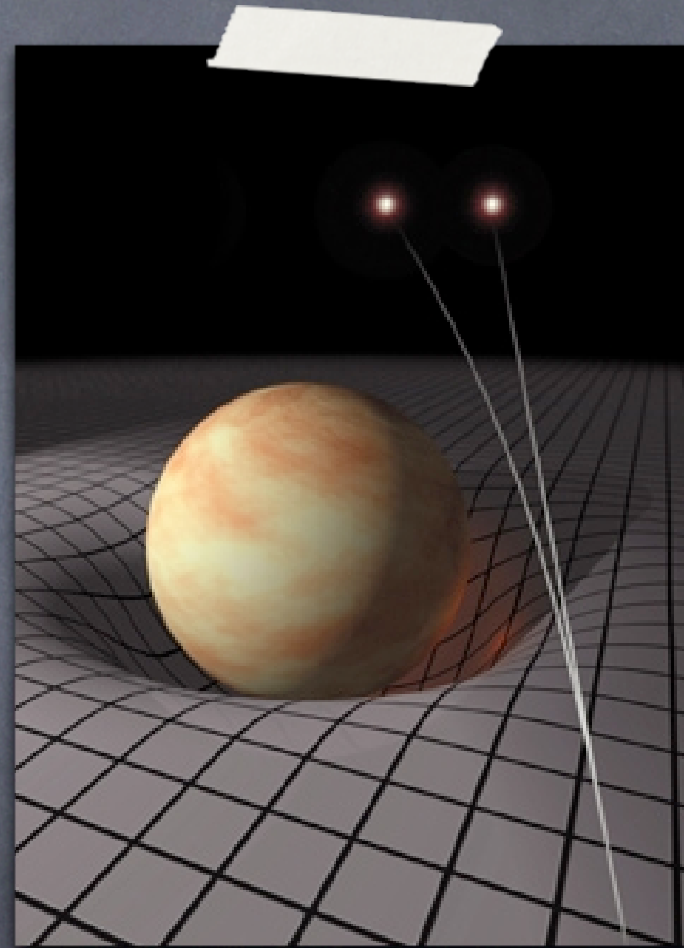
$$G_{ab} = kT_{ab}$$

$$R_{ab} - \frac{1}{2}Rg_{ab}, \quad R = R^a_a$$

$$\frac{8\pi G}{c^4} = 2 \times 10^{-48} \text{sec}^2/\text{g cm}$$



Spacetime grips mass, telling it how to move; mass grips spacetime, telling it how to curve.



- John Archibald Wheeler